

# Crises in Repo Markets with Adverse Selection

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# Outline

- 1 The model.
- 2 Analysis.
  - Sunny regime
  - Rainy regime
  - Rainy steady state
- 3 Discussion and Conclusion.

## Question

How can the worsening of a small part of the loan market lead to a crash as well as a prolonged crisis in secondary loan prices, bank equity prices, and lending activity?

# Answers

- **Method:** A model with banks, short-term repurchase financing and adverse selection.
- **Results:** initial crash (very bad), followed by adverse selection (somewhat bad).
- **Policy (tentative!):**
  - ▶ Emergency purchases in  $t = 0$  very good.
  - ▶ After  $t > 0$ , it may be better to leave the market as is.

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## Overview of the model:

- Banks and only banks can issue loans.
- Loans are long-term contracts.
- Banks use short-term repurchase agreements (“repos”) to leverage equity.
- Heterogeneous leveraging ability.
- Primary loan market (“loan-generation”).
- Secondary market, where loans can be traded among banks and sold by short-term lenders.
- Loans may differ in quality. Private info to bank. Adverse selection on secondary market.
- Transition from “sunny” to “rainy” regime.

# Time, Regimes and Households

- Time:  $t = \dots, -2, -1, 0, 1, 2, \dots$
- Regimes: “Sunny”, “Rainy”.
  - ▶ Start “sunny”.
  - ▶ Surprise transition to “rainy” forever.
  - ▶ Date  $t = 0$ : first date of “rainy”.
- Households:  $R \geq 1$ ,

$$U = E \left[ \sum_{t=-\infty}^{\infty} R^{-t} c_t \right]$$

- Zero endowment.  $c_t$  can be negative.

## Two linear technologies (“loans”)

- “good” (g), “bad” (b)
- Require one unit of input at date  $t$ .
- Terminate with probability  $1 - \kappa$ .
- Otherwise: pay dividend forever:
  - ▶ “Good”:  $d_s$ , while “sunny.  $d_g$  while “rainy”.
  - ▶ “Bad”:  $d_s$ , while “sunny.  $d_b < d_g$  while “rainy”.



# Banks

- Only banks can issue and collect on loans.
- Primary market: creation of new loans.

$$P(\text{"good"}) = \alpha$$

- Lots of tiny loans. Probability = fraction. LLN.
- Secondary market: trade loans. Endogenous market price  $p_t$ .

$$P(\text{"good"}) = \tilde{\alpha}_t \text{ (endogenous)}$$

- Only holding bank observes dividends.
  - ▶ "Sunny": no distinction.
  - ▶ "Rainy": holding bank knows "good" from "bad".

# Leverage and short-term lending

- Households create new banks of type  $\tau \in [0, 1]$  each period, with unlevered equity density  $f(\tau)$ : exogenous.
- Banks: “born” with type  $\tau \in [0; 1]$ .
- “Haircut” or “Leverage”.
- Loans  $L$ . Market value  $p_t$ .
- Repurchase agreements or repos:
  - ▶ borrow short term, post collateral in excess of loan.
  - ▶ borrow up to  $(1 - \tau)p_t L$ , repay with return  $R$  next period.
- Banks exit with probability  $1 - \gamma$ . They then sell their portfolio and pay their shareholders.

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## Leverage (given: $e = 1$ .)

- Equity:  $e$ .
- For  $L$  loans, can borrow (“repo”)  $(1 - \tau)pL$ .
- Primary market:

$$L = e + (1 - \tau)pL$$

or

$$L = \frac{1}{1 - (1 - \tau)p} e$$

- Secondary market:

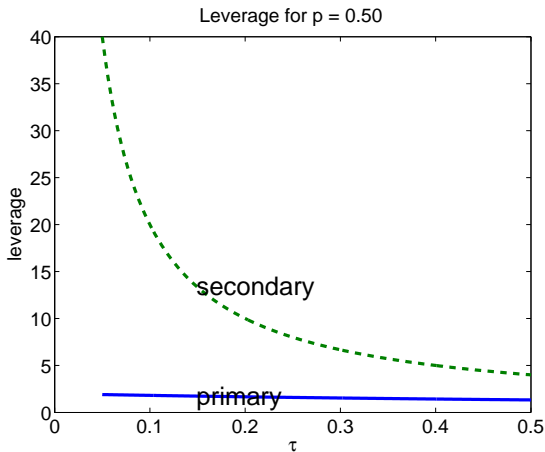
$$pL = e + (1 - \tau)pL$$

or

$$L = \frac{1}{\tau p} e$$

- Same for  $p = 1$ .

# Leverage



# Investment strategy

- Parameters such that it is good to be a bank, but not infinitely so.
- Always reinvest dividends.
- Get maximal leverage. Use new repos to pay off old repos.
- When exiting:
  - ▶ Sell all assets.
  - ▶ Pay off shareholders.

# Loans and stock price

- $p = 1$ .
- Loans:

$$L(\tau) = \frac{f(\tau)}{\tau(1 - \gamma R) - \gamma(d_s - r)} \quad (1)$$

- Assumption:

$$\tau(1 - \gamma R) - \gamma(d_s - r) > \epsilon > 0 \quad (2)$$

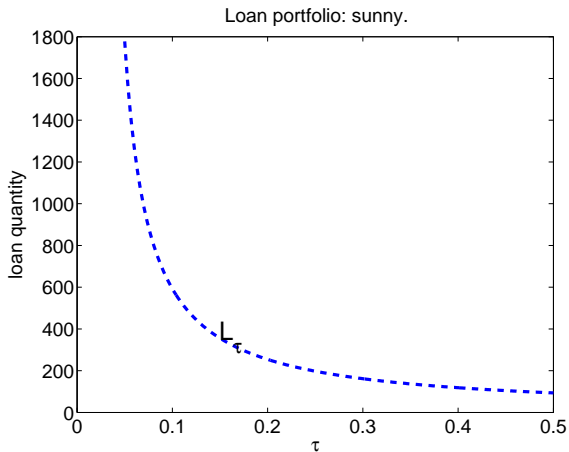


## Parameters for Illustration

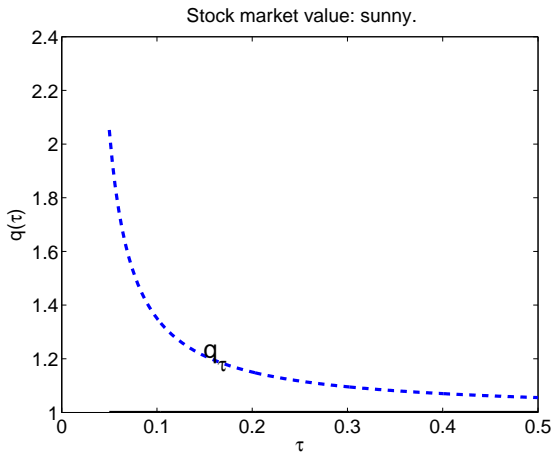
$\alpha$	P("good")	0.9
$\gamma$	continuation prob. for banks	0.95
$R$	refinancing return	1
$\kappa$	continuation prob. for loans	0.9
$\underline{\tau}$	inverse of max. leverage	0.05
$\epsilon$	(technical)	0.0013
$d_g$	dividends, "good"	0.113
$d_b$	dividends, "bad"	0
$d_s$	dividends, "sunny"	$= \bar{d}$
$r = R - \kappa$	required rate of return	0.1
$\bar{d}$	av. "rainy" dividends	0.1013

Bank creation: uniform density  $f(\tau)$  on  $\tau \in [0.05, 0.5]$ , with  $\int f(\tau) = 1$ .  
 I.e.: leverage between 2 and 20.

# Loans



# Stock price



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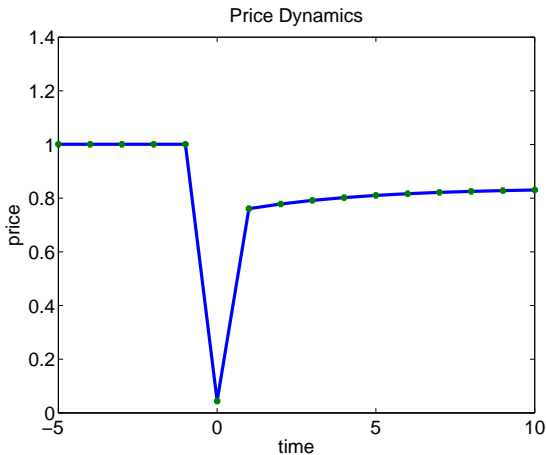
# Rainy period

- Banks will sell bad loans before selling good loans.
- Banks will sell all bad loans, if price exceeds their value.

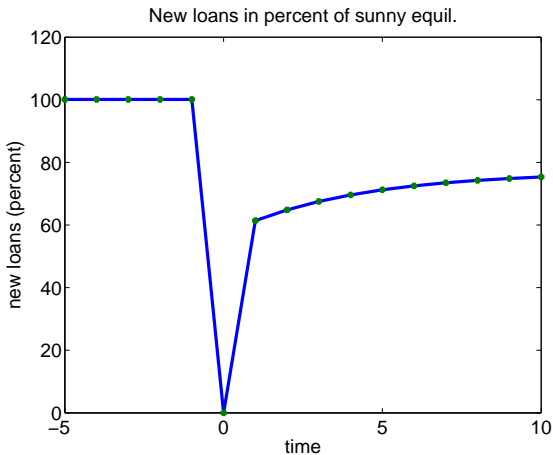
## Two phases

- $t = 0$ : **Cash-in-the-Market**. Price below value of bad loan. Emergency selling only.
- $t > 0$ : **Adverse Selection**. Price above value of bad loan. All continuing banks sell all their bad loans.

# Price dynamics (speed: conjectured)



# New loan dynamics (speed: conjectured)

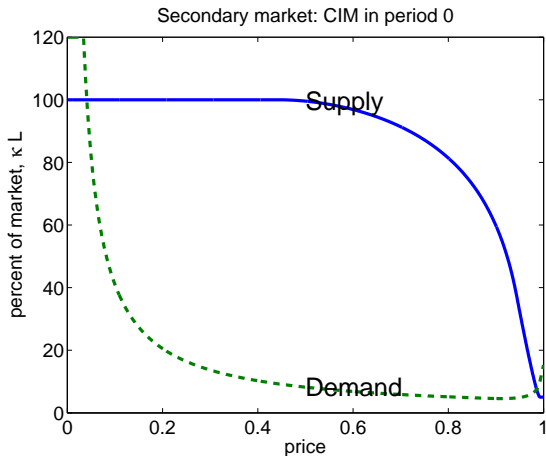




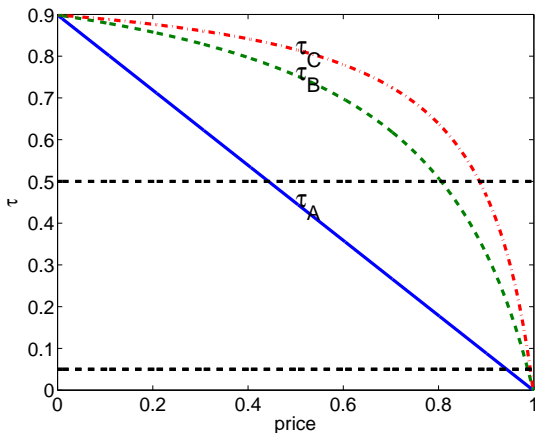
## Cash in the Market Pricing, $t = 0$

- Must have:  $p_0 < 1$ .
- Banks have been highly leveraged. Use new loans at  $p = 1$  to pay off old loans. But now,  $p_0 < 1$ .
- Equilibrium: price  $p_0$ , supply = demand,  $\tau_A, \tau_B, \tau_C$ .
- $\tau \leq \tau_A$ : bankruptcy.
- $\tau_A < \tau \leq \tau_B$ : sell all bad loans, some good loans.
- $\tau_B < \tau \leq \tau_C$ : sell some bad loans.
- $\tau_C \leq \tau$ : buy loans.
- Numerics:  $p_0 = 0.044$ .
- Price is below value of bad loan, all sell all loans:  $\tau_A > 0.5$ .  
Demand: only the new banks.

# Cash in the Market Pricing, $t = 0$



# Cash in the Market Pricing, $t = 0$



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## Adverse selection, $t > 0$ . Steady state.

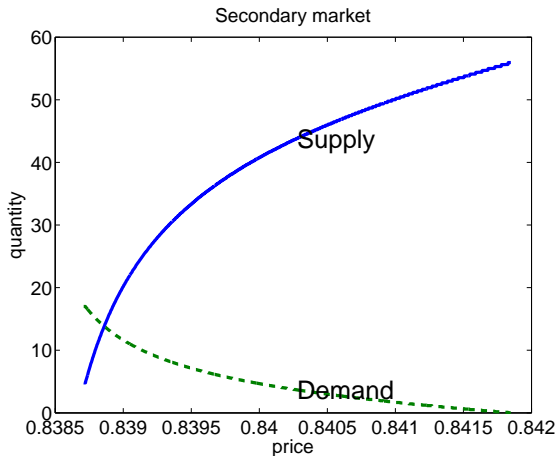
- Price above value of bad loan.
- All continuing banks sell all their bad loans.
- Mix on secondary market:

$$\tilde{\alpha} = \frac{(1 - \gamma)\alpha}{1 - \gamma\alpha} < \alpha$$

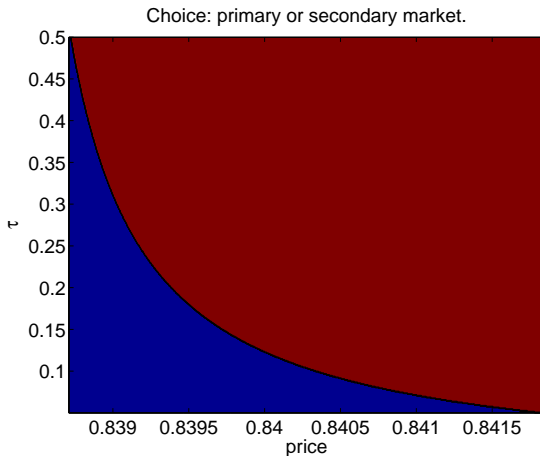
Numerics:  $\alpha = 0.9$ , but  $\tilde{\alpha} = 0.31$ .

- High  $\tau$  (low leverage): only primary market.
- Low  $\tau$  (high leverage): only secondary market.

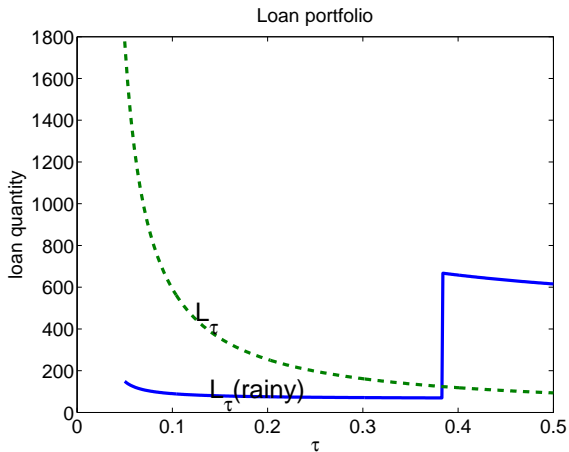
# Adverse selection steady state



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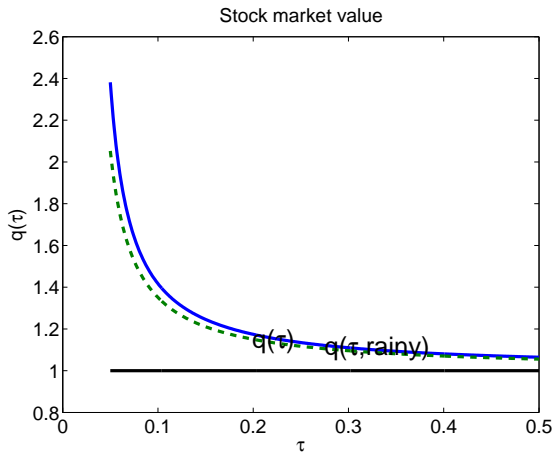


# Adverse selection steady state





# Adverse selection steady state



# Numerical results

$\tilde{\alpha}$	0.31
$\tilde{\alpha}_{\text{prim}}$	0.984
$\tilde{\alpha}_{\text{sec}}$	0.756
$\rho_0$	0.044
$\rho_{(\text{rainy})}$	0.839
$\tau_{\text{rainy}}^*$	0.384
$L_{\text{rainy}}/L_{\text{sunny}}$	77.0 %

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# What can policy do?

- Less leverage?
  - ▶ Reduces  $L$  in “sunny” times.
  - ▶ Crash at  $t = 0$ , unless leverage restriction is then relaxed.
- Buy assets.
  - ▶ Excellent in  $t = 0$ !
  - ▶ In  $t > 0$ ?
- Lower haircut, i.e. reduce  $\tau$ .
  - ▶ Won't help much.
  - ▶ Not the issue in  $t = 0$ .
- Lower interest rates  $R$ .
- Reschedule loans. Very powerful in  $t = 0$ .
- Adverse selection steady state somewhat worse, but not much than “sunny” with  $d$ , but not much. Easy to over-correct! It may be better to live with some inefficiencies.

# Conclusions

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